

# Biomolecular modeling IIII

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# Enhanced sampling

How to save time, and time is money

# Problem

with normal nanosecond length MD simulations:

It is difficult to overcome **barriers** to conformational transitions, and only conformations in the neighborhood of the initial structure may be sampled, even if some other (different) conformations are more relevant, i.e. have lower **free energy**

Special techniques are required to solve this problem.

## Note – do not be afraid of Arrhenius

How often does something happen (in a simulation)?

$k = A \times \exp[-E_A/kT]$ , let us have  $A = 1 \times 10^9 \text{ s}^{-1}$

$E_A$ kcal/mol	$k$ 1/s	$1/k$ $\mu\text{s}$
1	$0.19 \times 10^9$	0.005
3	$6.7 \times 10^6$	0.15
5	$0.24 \times 10^6$	4.2
7	$8.6 \times 10^3$	120

So, if the process has to overcome a barrier of 5 kcal/mol, we will have to simulate for 4  $\mu\text{s}$  to see it happen **once** on average.

# Replica-exchange molecular dynamics

REMD (or **parallel tempering**) – method to accelerate the sampling of configuration space, which can be applied even if the configurations of interest are separated by high barriers.

Several (identical) replicas of the molecular system are simulated at the same time, with **different temperatures**.

The coordinates+velocities of the replicas may be switched (**exchanged**) between two temperatures.

## Probability of replica exchange

The probability of the replica exchange between  $T_1$  and  $T_2$  is determined in (regular) time intervals from the instantaneous potential energies  $U_1$  and  $U_2$  in the corresponding simulations as

$$\mathcal{P}(1 \leftrightarrow 2) = \begin{cases} 1 & \text{if } U_2 < U_1, \\ \exp \left[ \left( \frac{1}{k_B T_1} - \frac{1}{k_B T_2} \right) \cdot (U_1 - U_2) \right] & \text{otherwise.} \end{cases}$$

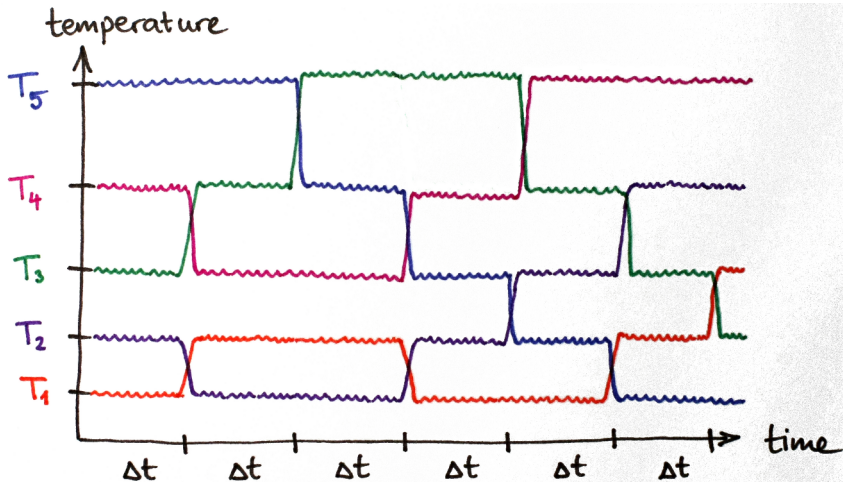
Then, if  $\mathcal{P}(1 \leftrightarrow 2)$  is **larger than a random number** from  $(0, 1)$ , the replicas in simulations at  $T_1$  and  $T_2$  are exchanged.

## Setup of the simulation of replicas

Simulated one replica at the temperature of interest ( $T_1 = 300$  K) and several other replicas at higher temp. ( $T_1 < T_2 < T_3 < \dots$ ).

After (say) 1000 MD steps, attempt exchanges  $1 \leftrightarrow 2$ ,  $3 \leftrightarrow 4$  etc., and after next 1000 steps do the same for  $2 \leftrightarrow 3$ ,  $4 \leftrightarrow 5$  etc. so only try to exchange replicas at “neighboring” temperatures

# Setup of the simulation of replicas





# Advantages of REMD

- due to the simulations at high temperatures
- faster sampling and more frequent crossing of energy barriers
- correct sampling at all temperatures obtained, above all at the (lowest) temperature of interest
- increased computational cost (multiple simulations) pays off with **largely** accelerated sampling
- simulations running at different temperatures are **independent** except at attempted exchanges → **easy parallelization**
- first application – protein folding (Sugita & Okamoto, Chem. Phys. Lett. 1999)

## Choice of temperatures and disadvantages of REMD

For protein/water systems with all bond lengths constrained:

- $N_{\text{dof}} \approx 2N$  ( $N$  – number of atoms)
- average probability is related to  $T_2 - T_1 = \varepsilon T_1$  as

$$\overline{\mathcal{P}(1 \leftrightarrow 2)} \approx \exp[-2\varepsilon^2 N]$$

- set of temperatures may be designed to suit the problem

Disadvantages of parallel tempering REMD

- large number of atoms: low exchange probability  
→ low efficiency
- high temperature – sensitive biostructures may not survive  
(membranes etc.)

how to apply the replica-exchange idea and avoid these issues?

## Hamiltonian replica exchange – HREX

also called ‘Replica exchange with solute tempering’ (REST)

$$P = \exp \left[ -\frac{U}{kT} \right] = \exp [-\beta U]$$

- note:  $\frac{1}{2} U$  would be the same as  $2 T$
- force field energy  $U$  is combined from many individual terms
  - let us **scale selected terms** (not all of them!)
  - is not possible for temperature scaling (a single  $T$ )
  - ‘heating’ of a (small) part of the system
  - typically, a group of atoms – a ligand, or several AAs. . .

## Hamiltonian replica exchange – HREX

Simulations 1 and 2 are performed  
with different force fields  $U_1$  and  $U_2$

How to calculate the probability of exchange?  
( $q_1$  and  $q_2$  – coordinates of atoms in simulations 1 and 2)

$$\Delta = \frac{U_1(q_2) - U_1(q_1) - U_2(q_1) + U_2(q_2)}{kT}$$
$$\mathcal{P}(1 \leftrightarrow 2) = \begin{cases} 1 & \text{if } \Delta \leq 0, \\ \exp[-\Delta] & \text{otherwise.} \end{cases}$$

Then, if  $\mathcal{P}(1 \leftrightarrow 2)$  is larger than a random number from  $(0, 1)$ , the replicas in simulations with  $U_1$  and  $U_2$  are exchanged.

## HREX – a good variant

- divide the system into two parts:
- **hot** – small, will be subject to extended sampling
- **cold** – all of the rest

Generate replicas with different  $\lambda_m < 1$ , modify parameters in **hot**:

- scale the charges by  $\sqrt{\lambda_m}$
- scale the LJ depths  $\varepsilon$  by  $\lambda_m$
- additional scaling of dihedral angles

Then, the ‘effective’ temperatures are

- inside **hot**:  $T/\lambda_m > T$
- interactions between **hot** and **cold**:  $T/\sqrt{\lambda_m}$
- inside **cold**:  $T$  is retained

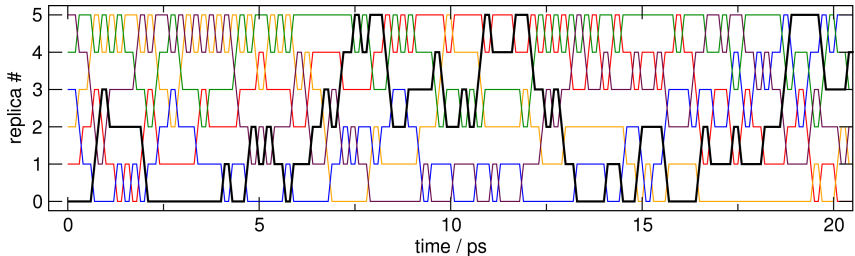
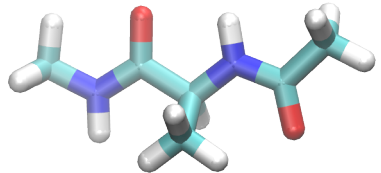
# HREX

## Meaning of temperature

- kinetic energy  $\leftarrow$  velocities
  - does not change, is the same in **hot** and **cold** (300 K)
  - simulation settings need not be adjusted (time step!)
  - unlike in parallel tempering
- factor affecting the population of states
  - we play with this

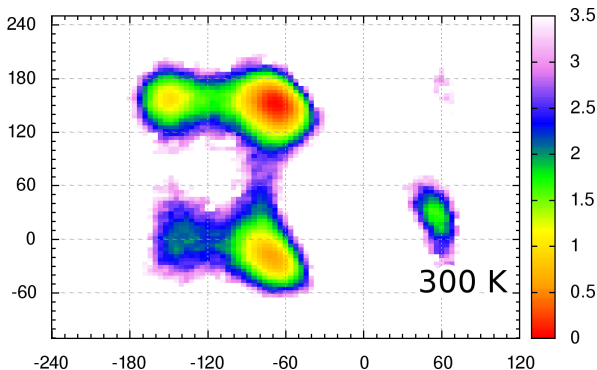
# HREX – example – solute tempering

- alanine dipeptide – 22 atoms,  
1 pair of  $\varphi - \psi$
- 5 replicas,  $\lambda = 1 \dots 0.18$   
i.e.  $T_m = 300 \dots 1700$  K
- exchange every 0.1 ps,  
observed  $\overline{P} = 0.25 - 0.50$



# HREX – example

Solute tempering – dialanine – replica #0

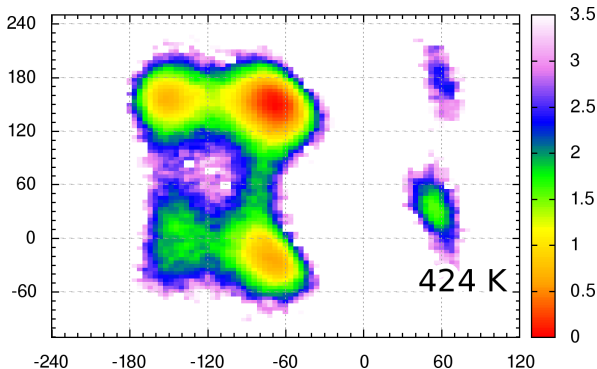


$\varphi - \psi$  in degrees,  $\Delta F$  in kcal/mol



# HREX – example

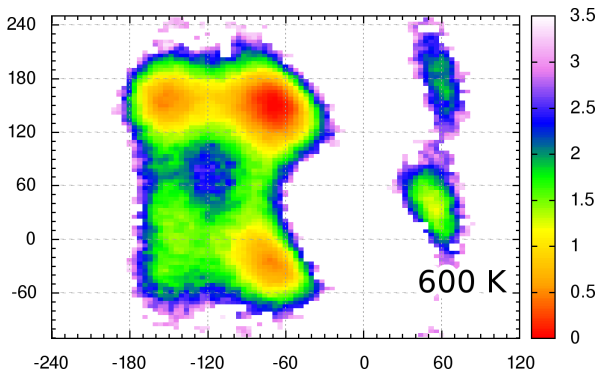
Solute tempering – dialanine – replica #1



$\varphi - \psi$  in degrees,  $\Delta F$  in kcal/mol

# HREX – example

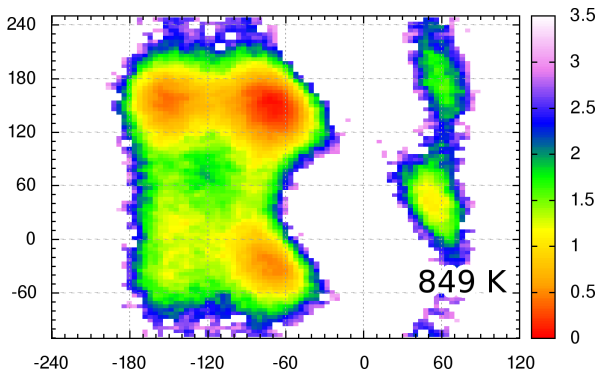
Solute tempering – dialanine – replica #2



$\varphi - \psi$  in degrees,  $\Delta F$  in kcal/mol

# HREX – example

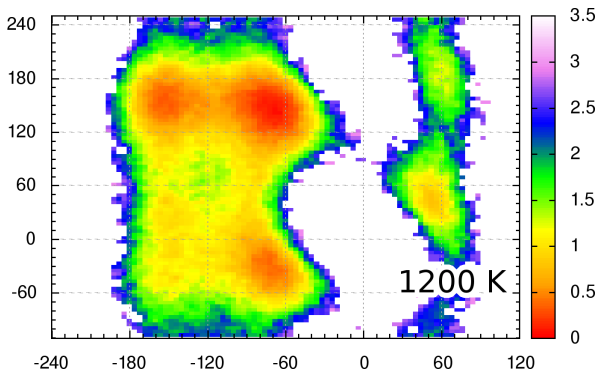
Solute tempering – dialanine – replica #3



$\varphi - \psi$  in degrees,  $\Delta F$  in kcal/mol

# HREX – example

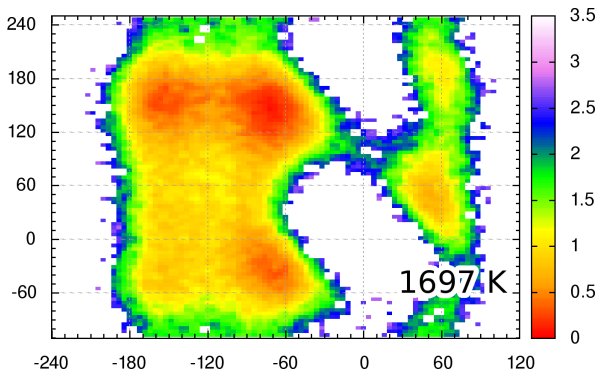
Solute tempering – dialanine – replica #4



$\varphi - \psi$  in degrees,  $\Delta F$  in kcal/mol

# HREX – example

Solute tempering – dialanine – replica #5



$\varphi - \psi$  in degrees,  $\Delta F$  in kcal/mol

## Methods using biasing potentials

Other approaches use a different idea:

It is easy to introduce an additional contribution to the potential energy of the molecule

Example – the extra potential may **force** the molecule over an energy barrier, to explore other conformations

It is ‘unrealistic’ – we do not simulate a real molecule but this **bias** may be removed by a right post-processing

Note: use of NMR-based distance restraints in MD simulations  
→ ‘NMR-refined’ structure of the molecule (e.g. PDB ID 1AC9)

# Metadynamics

- aimed at reconstructing the multidimensional free energy of complex systems (Laio & Parrinello 2002)
- based on an artificial dynamics (metadynamics) performed in the space of a few collective variables  $S$  (e.g. normal modes)
- at regular time intervals during the simulation, an additional biasing energy function is added to the force field
  - a Gaussian that is centered on the current structure

using quotations by Alessandro Laio

## Metadynamics – how it works

a new Gaussian is added at every time interval  $t_G$ ,  
and the biasing potential at time  $t$  is given by

$$V_G(S(x), t) = \sum_{t'=t_G, 2t_G, 3t_G, \dots} w \cdot \exp \left[ -\frac{(S(x) - s_{t'})^2}{2 \cdot \delta s^2} \right]$$

$w$  and  $\delta s$  – height and width of the Gaussians

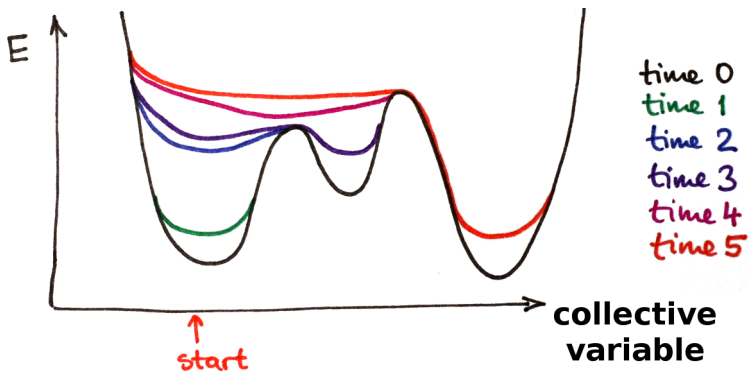
$s_t = S(x(t))$  – value of the collective variable at time  $t$

In the course of the simulation, this potential is filling the minima  
on the free energy surface that the system is traveling through

So, the MD has a **memory** via the biasing potential



# Metadynamics – what it looks like



<https://www.youtube.com/watch?v=IzEBpQ0c8TA>

<https://www.youtube.com/watch?v=iu2GtQAyoj0>

# Properties of metadynamics

Metadynamics – to explore new reaction pathways,  
accelerate rare events,  
and also to estimate the free energies efficiently.

- The system escapes a local free energy minimum through the lowest free-energy saddle point.
- The dynamics continues, and all of the free-energy profile is filled with the biasing Gaussians.
- At the end, the sum of the Gaussians provides the **negative of the free energy**.

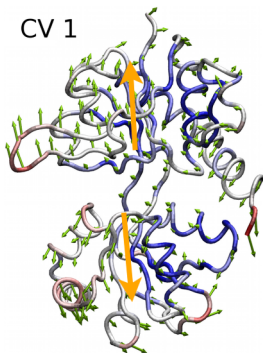
# Properties of metadynamics

Crucial task – prior to simulation: identify the **collective variables** of interest  
that are difficult to sample because of high barriers

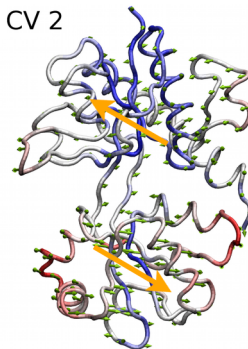
These variables  $S(x)$  are functions of the coordinates of the system;  
practical applications – up to 3 such variables,  
and the choice depend on the process being studied.

Typical choices – principal modes of motion obtained with PCA  
Still, the choice of  $S$  may be difficult

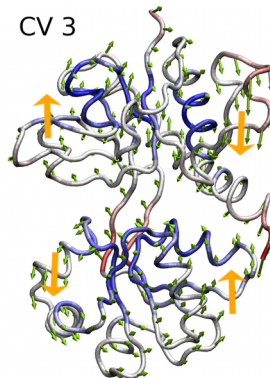
## Example – opening of a protein binding pocket



clamshell



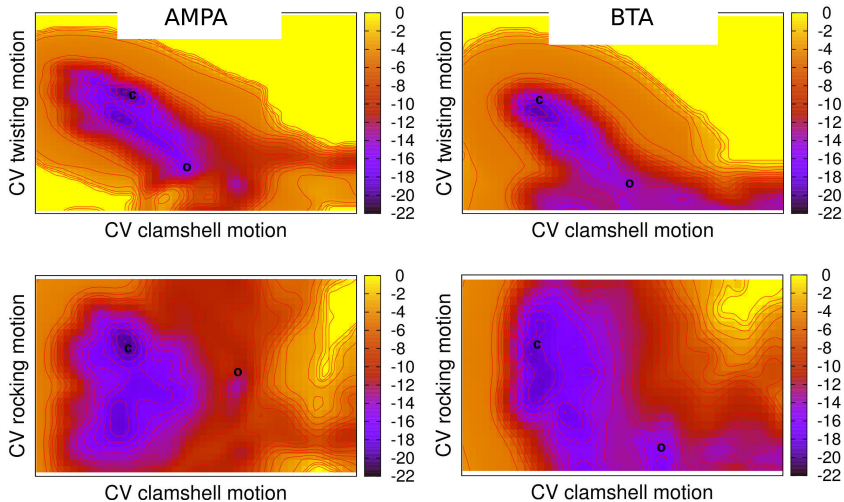
twisting



rocking

courtesy Tino Wolter

## Example – opening of a protein binding pocket



courtesy Tino Wolter

## Enhanced sampling methods – comparison

Biasing potential methods – metadynamics, umbrella sampling

- required: a priori choice of reaction coordinate(s) to be biased
- problem – success depends on that choice, possibly non-trivial

REMD with **parallel tempering**

- + no such required, can be used rather blindly
- – all of the system heated  $\rightarrow$  may destroy something
- – no knowledge of the system may be embedded
- – poor efficiency for big systems:  $\overline{\mathcal{P}(1 \leftrightarrow 2)} \approx \exp[-2\epsilon^2 N]$   
 $\rightarrow$  **critical problem**

## Enhanced sampling methods – comparison

### Hamiltonian replica exchange (HREX)

- in intermediate position
  - between metadynamics/US and REMD-PT
- simpler to use than metadynamics/US
  - results depend not so strongly on the choices to be made
- efficiency does not depend on the overall system size

# Free energy simulations



# Motivation

physical quantities of prime interest in chemistry?

free energies – Helmholtz  $F$  or Gibbs  $G$

- determine whether processes (reactions) run spontaneously or not
- holy grail of computational chemistry,  
both for their importance  
and because they are difficult to calculate

# Convergence issue

(all of the formulas come from statistical thermodynamics)

– especially desperate for free energies:

$$F = k_B T \cdot \ln \left\langle \exp \left[ \frac{E}{k_B T} \right] \right\rangle$$

serious issue – the large energy values enter an exponential,  
and so the high-energy regions may contribute significantly!

→ if these are undersampled, then free energies are wrong

– calculation of free energies impossible, **special methods needed!**

# Tackling the issue

two fundamental approaches:

free energy perturbation and **thermodynamic integration**

several computational tricks for particular types of reactions:

**alchemical simulations** or **umbrella sampling**

important: not necessary to find the absolute value of free energy;

for a chemical reaction, we only need

the **free energy difference** ( $\Delta F$ ,  $\Delta G$ ) of reactant and product

“reaction” – not necessarily chemical bonds created or broken

- ligand binding a protein

- passage of a molecule/ion through membrane

- protein folding

...

# Thermodynamic integration

Free energy as function of **reaction coordinate**  $\lambda$ :  $F = F(\lambda)$ ,  
with  $\lambda = 0$  for reactant,  $\lambda = 1$  for product

$$\Delta F = F(1) - F(0) = \int_0^1 \frac{\partial F(\lambda)}{\partial \lambda} d\lambda$$

Free energy is a state function

- the result is **independent of the chosen path**  $0 \rightarrow 1$
- reaction coordinate may be even an unphysical process
- change of chemical identity of atoms (alchemical simulations)

$$\Delta F = \int_0^1 \left\langle \frac{\partial E_\lambda}{\partial \lambda} \right\rangle_\lambda d\lambda$$

Essence of TI – the average of derivative of total MM energy  $E$   
is evaluated in the simulation **directly**

## How to do it practically

- perform a MD simulation for each chosen value of  $\lambda$ :
  - usually, equidistant values in the interval  $(0,1)$  are taken:  
 $0, 0.05, \dots, 0.95$  and  $1$
- each of these simulations produces a value of  $\langle \frac{\partial E}{\partial \lambda} \rangle_\lambda$ 
  - we obtain the derivative of  $F$  in discrete points for  $\lambda \in (0, 1)$
- this function is integrated numerically,
  - the result is the desired free energy difference  $\Delta F$
- how many “windows”, or  $\lambda$  values shall we choose?
  - we would like to have as few windows as possible,  
without compromising numerical precision
  - inaccuracy may be due to the numerical integration

# Computational alchemy

TI looks complicated, but it is rather straightforward,  
– common simulation programs run TI conveniently

## Computational alchemy

– change of chemical identities of atoms or functional groups

Using a parameter  $\lambda$ , the force-field parameters of state 0 are changed to those of state 1 gradually:

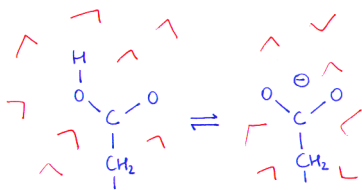
$$E_{\lambda} = (1 - \lambda) \cdot E_0 + \lambda \cdot E_1$$

# Advantages of TI

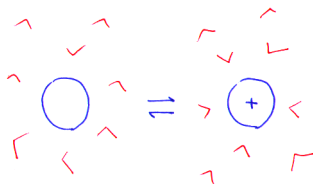
- evaluate the derivative of energies,  
no need to sample for the (large) total energies first
- it is not important what happens outside of the region  
where the reaction takes place (no contrib. to  $E_1 - E_0$ )
- the ensemble of structures that have to be sampled thoroughly  
is much smaller, and shorter simulation length is required

# Examples

deprotonation of amino acid



ionization of a molecule



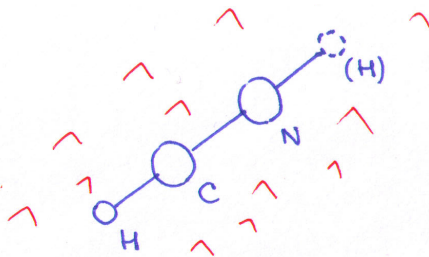
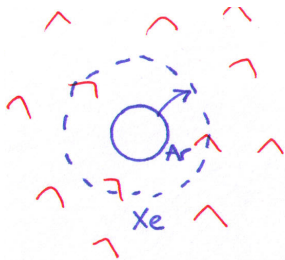


# Examples

hydration free energy difference of:

argon and xenon

HCN and CNH



## Example

The hydration free energy difference of argon and xenon

Let us interpolate between the parameters for the two elements:

$$\varepsilon_{\lambda} = (1 - \lambda) \cdot \varepsilon_0 + \lambda \cdot \varepsilon_1$$

$$\sigma_{\lambda} = (1 - \lambda) \cdot \sigma_0 + \lambda \cdot \sigma_1$$

In the simulation, we start from  $\lambda = 0$ , i.e. an argon atom, and change it in subsequent steps to 1.

For each step (**window**), we perform an MD simulation with the corresponding values of the vdW parameters, and evaluate the free energy derivative

## Example

Free energy of hydration of rare gas (neon)

van der Waals parameters of the neon are gradually switched off by means of  $\lambda$ , so that the atom is effectively disappearing

The derivative of total energy with respect to  $\lambda$  is evaluated for 21 values of  $\lambda$  ranging from 0 to 1.

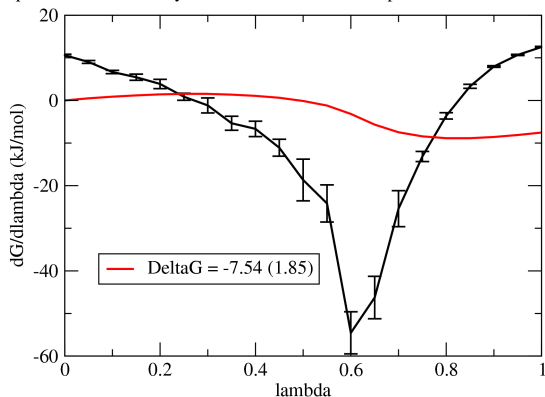
Then, TI gives the Gibbs energy difference of two states:

- a neon atom in water
- no neon atom in water  $\equiv$   
 $\equiv$  a neon atom outside of the solution, in vacuo

# Example

## Neon atom to nothing, in TIP3P water

equilibration: normality on 85% confidence level. production: error < 5 kJ/mol



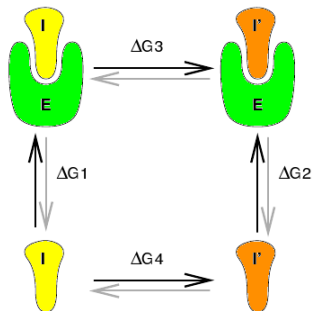
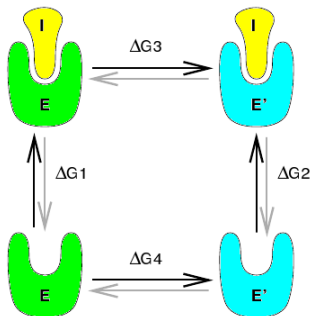
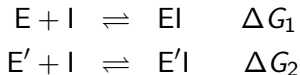
## Differences of differences

Often – we are interested not in the absolute free energies  
and not even in the reaction free energies,  
rather, in the **difference** ( $\Delta$ ) of reaction free energies ( $\Delta F$ )  
of two similar reactions:

$$\Delta\Delta F \text{ or } \Delta\Delta G$$

## Reaction free energy difference

Example left: binding of an inhibitor molecule I to an enzyme E, difference of binding free energies to similar enzymes E and E':



## Reaction free energy difference

The simulation of the ligand binding process itself – very difficult  
(possibly large structural changes in the enzyme upon binding)

Solution of the problem – do not simulate the reaction of binding,  
rather, the alchemical transmutation of enzyme E to E'.

E to E' are very similar so this may be easy to do.  
(example: mutation of a single AA, e.g. leucine to valine)

Then, the structure of complexes EI and E'I may be similar as well,  
and the simulation may provide converged free energy.

## Reaction free energy difference

Free energy is a state function  $\rightarrow$  the sum of free energies around a **thermodynamic cycle** vanishes:  
(e.g. clockwise in figure left):

$$\Delta G_1 + \Delta G_3 - \Delta G_2 - \Delta G_4 = 0$$

The difference of binding free energies equals the difference of free energies calculated in alchemical simulations:

$$\Delta\Delta G = \Delta G_1 - \Delta G_2 = \Delta G_3 - \Delta G_4$$



# Geometric reaction coordinate

Sometimes, we need to know how the free energy changes along a geometric **reaction coordinate**  $q$

The free energy is then a function of  $q$

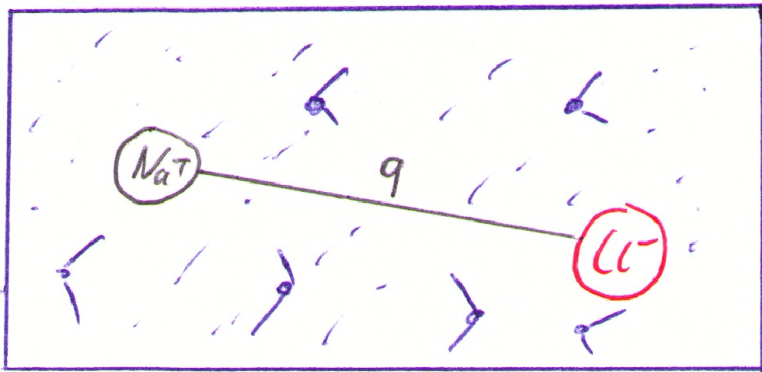
Such a function  $F(q)$  is called the **potential of mean force**.

Examples:

- distance between two particles in a dissociating complex
- the position of a proton for a reaction of proton transfer
- the dihedral angle when dealing with conformational changes

## Example

free energy of formation of an ion pair in solution:



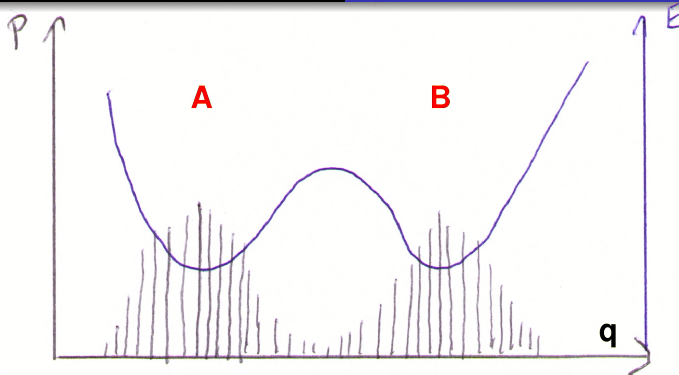
## Straightforward approach

We perform an MD simulation for the system,  
and then **count** how many times  $q$  takes the value  $q_1$ :  
calculate the probability  $P(q_1)$  of finding the system at  $q_1$

Then, the free energy difference of two states with  $q_1$  and  $q_2$  is

$$F_2 - F_1 = -k_B T \ln \frac{P(q_2)}{P(q_1)}$$

which contains the **equilibrium constant**  $P(2)/P(1)$



The problem:

If a high barrier has to be crossed to come from *A* to *B*,

a pure (**unbiased**) MD simulation will hardly make it

→ the high-energy region (barrier) is described poorly (for sure)

→ we may not obtain the product at all (possibly)

## Working principle

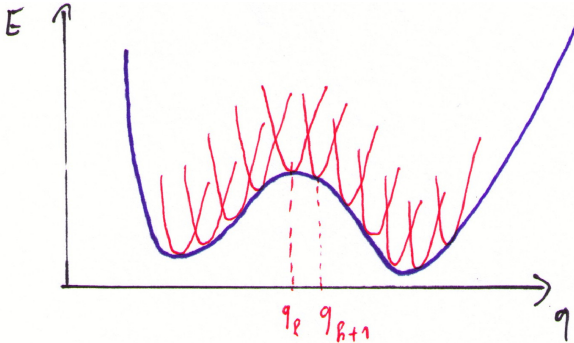
Apply an **additional potential**, also called **biasing potential** to restrain the system to values of reaction coordinate that would otherwise remain undersampled.

This is the principle of the **umbrella sampling**.

The additional potential will become a part of the force field, and it shall depend only on the reaction coordinate:  $V = V(q)$

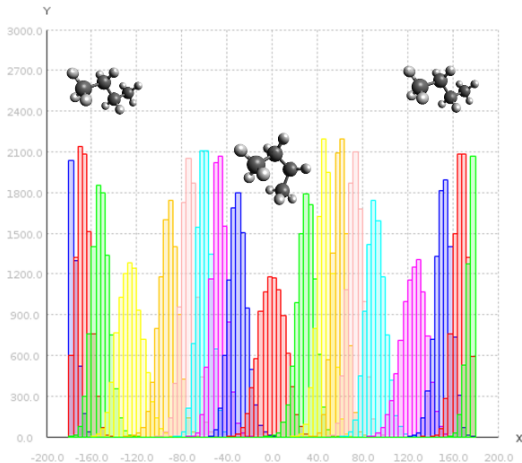
# Practical umbrella sampling

We can use this scheme efficiently, by way of moving a biasing **harmonic** potential along the reaction coordinate:



# Practical umbrella sampling

Example – probabilities from biased simulations – **histograms**



<http://people.cs.uct.ac.za/~mkuttel/images/projectImages/WHAM.png>

## Potentials of mean force

- We perform  $k$  simulations with biasing potentials  $V_k$ , which are designed to cover the interesting range of  $q$
- From each of the  $k$  simulations, we extract the **biased probability**  $P^*(q)$  of finding the system at the certain value of  $q$ 
  - this differs from the real, unbiased probability  $P(q)$
- We correct for bias to obtain the **unbiased free energy**  $F(q)$

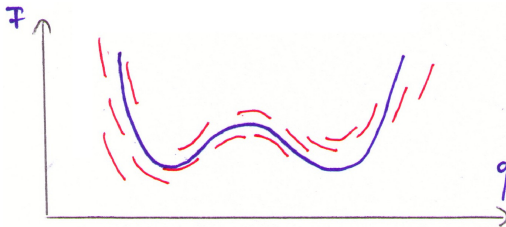
$$F_k(q) = -k_B T \ln P^*(q) - V_k(q) + K_k$$

where  $K_k$  is a constant shift that has to be determined



# Potentials of mean force

- the curves  $F_k(q)$  for simulations  $k$  and  $k + 1$  differ by a constant shift, difference of  $K$
- main task – match the pieces to provide a continuous curve
- one way – **fit** the values  $K_k$  to obtain a resulting  $F(q)$  curve that is as continuous and smooth as possible
- requirement – sufficient ‘overlap’ of the pieces  $F_k$  and  $F_{k+1}$
- **WHAM** method – included in modern simulation programs



# Molecular modeling in the drug design

# Drug design

- to construct new chemical compounds interacting in a defined way with natural materials – proteins, NA, carbohydrates. . .
- typical example – find a potent inhibitor of an enzyme, which does not interact harmfully with other substances in the organism
- typical difficulties:
  - the drug has to be a potent inhibitor
  - it must not interact with other enzymes (might be lethal)
  - it must not decompose too early (to reach destination)
  - its metabolites must not be (too) toxic

hard and \$\$\$ business

# Molecular docking

“Docking is a method which predicts the preferred orientation of one molecule to a second when bound to each other to form a stable complex.” Wikipedia

Typical pharmacological problem – find a ligand molecule to bind to a protein as strongly and specifically as possible

Good news: the binding site (pocket) is usually known  
– often, the active or allosteric place of the protein

Bad news:

- many DoF – transl., rot. and internal flex. of the ligand
- only a small number of molecules can be docked manually, once the binding mode of a similar molecule is known (and, even similar molecules sometimes bind differently)

# Molecular docking

a sequence of tasks:

- 1 Generate the pool of compounds to test – database of compounds, construction from a database of moieties,...
- 2 For each compound, find the binding mode. For this, try out several/many orientations and conformations (poses), and determine the most favorable
- 3 Evaluate the strength of the interaction.  
Accurate determination of  $\Delta G_{\text{bind}}$  impossible;  
instead, a **scoring function** is employed

# Molecular docking

Various levels of approximation may be employed

The simplest approach – exploit a database of molecules, and try to fit each molecule as a rigid body into the binding pocket

A natural expansion – consider the flexibility of the ligand

How to generate different configurations of the molecule?

- simple minimization or molecular dynamics
- Monte Carlo, perhaps combined with simulated annealing
- genetic algorithms

Efficient alternative – incremental construction of the ligand, which is partitioned into chemically reasonable fragments  
– natural account for the conformational flexibility of the molecule

# Molecular docking

problem of docking – it is all about sampling

No way to do molecular dynamics for every candidate molecule:

- MD takes much longer than what is affordable  
(would be OK for one ligand, but there are too many)
- MD would probably work only for quite rigid molecules moving relatively freely in the binding pocket (usually not the case)

Difference:

- If the goal is to dock a single molecule – a thorough search is affordable, involving MD, enhanced sampling. . .
- If we have to dock and assess many candidate ligands
  - simpler approaches have to be chosen
  - current state of the art – consider the flexibility of ligands
  - flexibility of protein (side chains) under development

# Scoring function

needed: extremely efficient way to quantify the strength of binding

- 1 to find the right binding mode of each ligand
- 2 to compare the strength of binding of various ligands.

the quantity of interest – binding free energy

problem with free energy methods – too inefficient for docking

what we need here – a simple additive function to approximate

$\Delta G_{\text{bind}}$ , which would give a result rapidly, in a single step



# Scoring function

$$\Delta G_{\text{bind}} = \Delta G_{\text{solv}} + \Delta G_{\text{conf}} + \Delta G_{\text{int}} + \Delta G_{\text{rot}} + \Delta G_{\text{t/r}} + \Delta G_{\text{vib}}$$

$\Delta G_{\text{solv}}$  – change of hydration (ligand, protein) upon binding

$\Delta G_{\text{conf}}$  – deformation energy of the ligand (forced by the pocket)

$\Delta G_{\text{int}}$  – ‘interaction energy’ – a favorable contribution

due to the specific ligand–protein interactions

$\Delta G_{\text{rot}}$  – loss of entropy due to the frozen rotations

approx.  $+RT \log 3 = 0.7$  kcal/mol per 3-state rotatable bond

$\Delta G_{\text{t/r}}$  – loss of trans. and rot. entropy upon association

– approx. the same for all ligands of similar size

$\Delta G_{\text{vib}}$  – change of vibrational modes – difficult, often ignored

# Scoring function

- a 'force field' for the free energy of binding
- problem – although approximative, it is still too costly
- usually, very simple constructions, looking over-simplified in comparison with MM force fields; example (Böhm, 1994):

$$\Delta G = \Delta G_0 + \Delta G_{\text{Hbond}} \cdot \sum_{\text{Hbonds}} f(R, \alpha) + \Delta G_{\text{ionpair}} \cdot \sum_{\text{ionpairs}} f'(R, \alpha) \\ + \Delta G_{\text{lipo}} \cdot A_{\text{lipo}} + \Delta G_{\text{rot}} \cdot N_{\text{rot}}$$

$\Delta G_{\text{Hbond}}$  – ideal hydrogen bond

$f(R, \alpha)$  – penalty function for a realistic hydrogen bond

$\Delta G_{\text{ionpair}}$  and  $f'(R, \alpha)$  – dtto for ionic contacts

$\Delta G_{\text{lipo}}$  – due to hydrophobic interaction; non-polar SA  $A_{\text{lipo}}$

$\Delta G_{\text{rot}}$  – due to a rotatable bond that freezes upon binding

# Scoring function

Further concepts present in other scoring functions:

- partitioning of the surface areas of both the proteins and the ligand into polar and non-polar regions, and assigning different parameters to the interactions of different kinds of regions (polar-polar, polar-nonpolar, nonpolar-nonpolar)
- statistical techniques to parametrize the scoring function

Problem – such s.f. only describe well ligands that bind tightly  
Modestly binding ligands

- of increasing interest in docking studies
- more poorly described by such functions

Possible solution – ‘consensus scoring’ – combining results from several scoring functions; performs better than any single s.f.

# Scoring function

Comment on accuracy

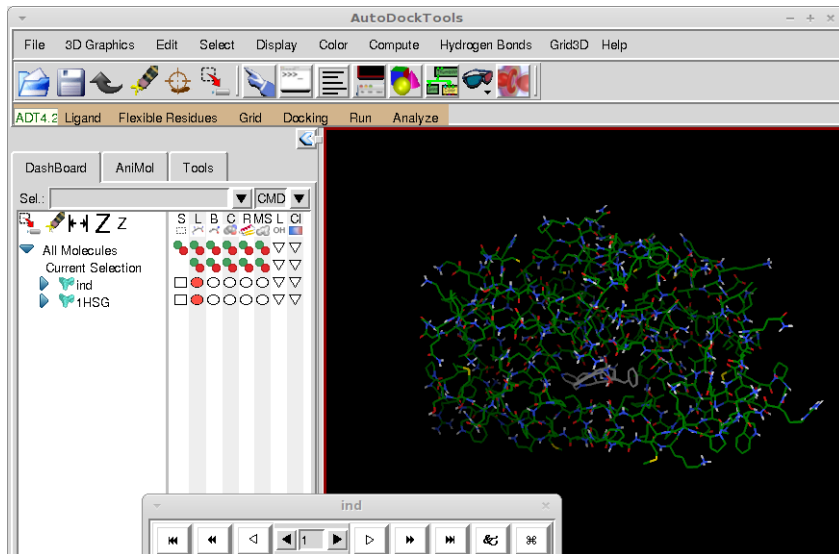
an error of  $\Delta G_{\text{bind}}$  of 1.4 kcal/mol

→ ten-fold increase/decrease of the inhibition constant

or: as little as 4.2 kcal/mol of  $\Delta G_{\text{bind}}$  lies

between a micro- and a nanomolar inhibitor

Therefore, the requirements on the accuracy of s.f.  
are actually rather big



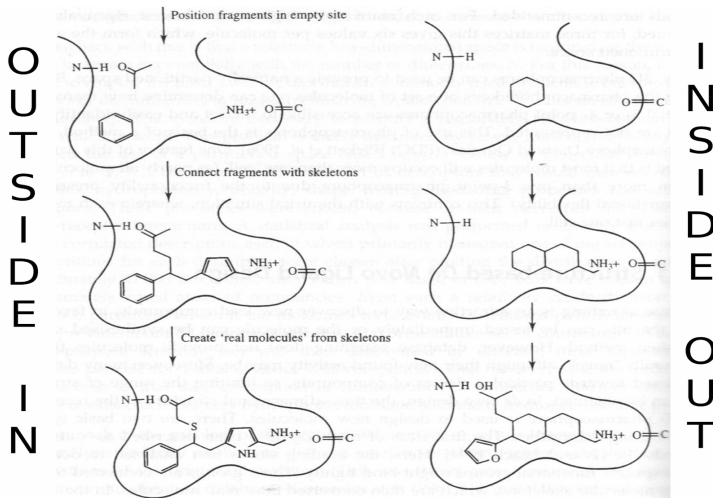
# De novo design of ligands

It may be a good idea to construct the ligand 'from scratch'  
– without relying on the content of a database.

2 basic types of *de novo* design:

- **outside-in**: Binding site is analyzed and tightly-binding ligand fragments are proposed. They are connected (db of linkers) → molecular skeleton of the ligand → actual molecule.
- **inside-out**: 'growing' the ligand in the binding pocket, driven by a search algorithm with a scoring function.

# De novo design of ligands



# Molecular docking

## Glossary of terms

- receptor / host / lock
- ligand / guest / key
- docking
- binding mode – position and orientation of ligand
- pose – a candidate for the binding mode
- scoring – determine how favorable a pose is
- ranking – of the poses to determine the binding mode