

# Biomolecular modeling I

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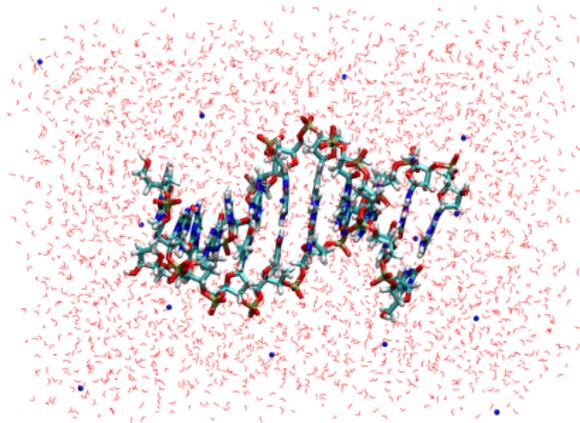
# Biomolecular simulation

Elementary body – **atom**

Each atom –  $x, y, z$  coordinates

“A protein is a set of coordinates.” (Gromacs, A. P. Heiner)

Usually – one molecule/complex of interest (e.g. protein, NA)



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**Simulation vs. reality**

One molecule instead of many

Tiny volume of  $\approx 10^{-21}$  L instead of  $\approx 10^{-5}$  L

Simulation of dynamics – short time scale of max.  $\approx 10^{-5}$  s

# Simulation vs. reality

Why should we want to simulate molecular systems?

Experiment – the molecule has its genuine properties

Simulation – we need a model to describe the interactions of atoms  
– the quality of the model is decisive

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Advantage of simulation – structure on atomic level defined

**Structure → function**

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Simulation – we need a model to describe the interactions of atoms  
– the quality of the model is decisive

Advantage of simulation – structure on atomic level defined

**Structure** → **function**

Combination of experiment and simulation – added value

# Molecular mechanics

classical description of molecules

# Motivation

- To investigate the **function** of biomolecules, we need to characterize its **structure** and **dynamics**.
- We will look how the molecules are moving
  - **M**olecular **D**ynamics

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- For this, we need to calculate the **forces** on atoms and the **energy** of the system
- Energy from quantum mechanics / quantum chemistry seemingly easy  $E = \langle \Psi | \hat{H} | \Psi \rangle$   
but not quite possible for large molecular systems

# Motivation

$$\left[ -\frac{\hbar^2}{2m_e\lambda^2} \nabla'^2 - \frac{e^2}{4\pi\epsilon_0\lambda r'} \right] \phi' = \mathcal{E} \phi'$$

$$[ij|kl] = \int d\mathbf{x}_1 d\mathbf{x}_2 \chi_i^*(\mathbf{x}_1) \chi_j(\mathbf{x}_1) r_{12}^{-1} \chi_k^*(\mathbf{x}_2) \chi_l(\mathbf{x}_2)$$

$$\begin{aligned} F_{\mu\nu} &= \int d\mathbf{r}_1 \phi_\mu^*(1) f(1) \phi_\nu(1) \\ &= \int d\mathbf{r}_1 \phi_\mu^*(1) h(1) \phi_\nu(1) + \sum_a^{N/2} \int d\mathbf{r}_1 \phi_\mu^*(1) [2J_a(1) - K_a(1)] \phi_\nu(1) \\ &= H_{\mu\nu}^{\text{core}} + \sum_a^{N/2} 2(\mu\nu|aa) - (\mu a|a\nu) \end{aligned}$$

$$|\Phi\rangle = c_0 |\Psi_0\rangle + \sum_{ra} c_a^r |\Psi_a^r\rangle + \sum_{\substack{a<b \\ r<s}} c_{ab}^{rs} |\Psi_{ab}^{rs}\rangle + \sum_{\substack{a<b<c \\ r<s<t}} c_{abc}^{rst} |\Psi_{abc}^{rst}\rangle + \dots$$

$$E_0^{(2)} = \sum_{a,b=1}^{N/2} \sum_{r,s=(N/2+1)}^K \frac{\langle ab|rs\rangle(2\langle rs|ab\rangle - \langle rs|ba\rangle)}{\epsilon_a + \epsilon_b - \epsilon_r - \epsilon_s}$$

## Idea of molecular mechanics

- often – well localized bonding orbitals (organic molecules)
- **idea** – similar bonds have similar strength and properties  
e.g. similar C–H  $\sigma$ -orbitals  $\rightarrow$  all C–H bonds are ‘similar’
- possibly by a harmonic spring? (the simplest possible function)

$$E(x) = \frac{1}{2}k(x - x_0)^2$$

$$F(x) = -\frac{\partial E(x)}{\partial x} = -k(x - x_0)$$

- 2 parameters  $k$  and  $x_0$  with defined meaning  
– can be obtained from spectroscopy

## Concept of (atom, bond... ) type

- let us use harmonic springs for covalent bonds
- we do not want to parametrize  $k$  and  $x_0$  each bond separately
- use just several sets  $(k, x_0)$ , for different **types** of bonds

Why can we expect such ‘unification’ to work?

# Concept of (atom, bond. . . ) type

## Spectroscopy

- every C–H bond: length 1.06–1.11 Å,  
frequency ca.  $3100\text{ cm}^{-1}$ , in any molecular environment

## Thermochemistry

- heat of formation – roughly additive:



# Concept of (atom, bond. . . ) type

How to identify the **atom types**? – chemical ideas

## Concept of (atom, bond... ) type

How to identify the **atom types**? – chemical ideas

i) hybridization

- different types for  $sp^3$  carbon (4 bonds) and  $sp^2$  C (3 bonds)
- different functions for bonds of types C–C, C=C and C≡C
- determine the parameters ( $k, x_0$ ) with some selected molecules, typical for the binding situation
- example: use  $C_2H_6$ ,  $C_2H_4$ ,  $C_2H_2$  and benzene for  $k, x_0$

## Concept of (atom, bond... ) type

How to identify the **atom types**? – chemical ideas

ii) polarity

- an atom bonded to electronegative atom – electron deficient  
→ affects its bonding to other atoms
- example: C–C bond in **O=CH–C**... is affected  
and needs to be parametrized differently from apolar C–C  
→ an atom type for carbonyl C introduced

Biomolecular force fields

– usually 20 types for C, 10 for N and 5 for O and H

## Concept of (atom, bond... ) type

AMBER types for carbon:

C - sp<sup>2</sup> C carbonyl group

CA - sp<sup>2</sup> C pure aromatic (benzene)

CB - sp<sup>2</sup> aromatic C, 5&6 membered ring junction

CC - sp<sup>2</sup> aromatic C, 5 memb. ring HIS

CK - sp<sup>2</sup> C 5 memb.ring in purines

CM - sp<sup>2</sup> C pyrimidines in pos. 5 & 6

CN - sp<sup>2</sup> C aromatic 5&6 memb.ring junct.(TRP)

CQ - sp<sup>2</sup> C in 5 mem.ring of purines between 2 N

CR - sp<sup>2</sup> arom as CQ but in HIS

CT - **sp<sup>3</sup>** aliphatic C

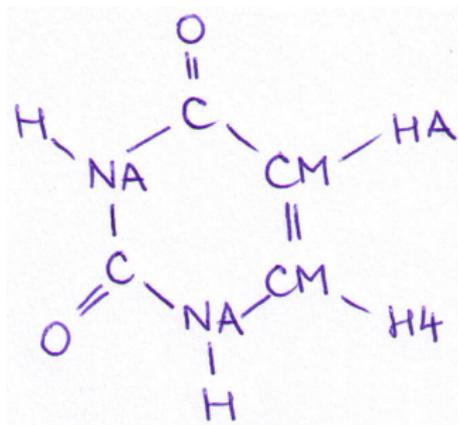
CV - sp<sup>2</sup> arom. 5 memb.ring w/1 N and 1 H (HIS)

CW - sp<sup>2</sup> arom. 5 memb.ring w/1 N-H and 1 H (HIS)

C\* - sp<sup>2</sup> arom. 5 memb.ring w/1 subst. (TRP)

# Concept of (atom, bond... ) type

AMBER atom types in a molecule of uracil



# Interactions between atoms

## Bonded

- mediated by, and resulting directly from covalent bonds
- cover all of the quantum-mechanical phenomena between pairs of atoms with effective potentials
- harmonic springs between atoms (also angles and dihedrals)

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## Non-bonded

- longer-range interactions
  - charge–charge (Coulomb) and van der Waals (vdW)
- between molecules and distant parts of one molecule

## Coulomb interaction

- idea – condense electrons in each atom with the nucleus  
→ **effective atomic charge**  $q_i = -Q_i + Z_i$ :

$$E_{QQ} = \frac{1}{2} \sum_{ij} \frac{q_i \cdot q_j}{R_{ij}}$$

- needs to be defined for **every atom**  
rather than atom type – this would be too crude
- from quantum-chemical calculations  
of typical (bio)molecular fragments
  - amino acid residues and peptide bonds for proteins
  - nucleobases, sugars and phosphate groups for DNA/RNA

# Coulomb interaction

How to calculate atomic charges?

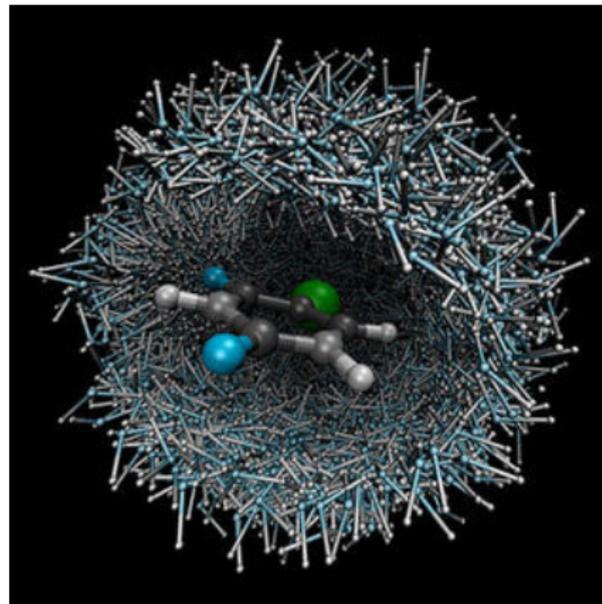
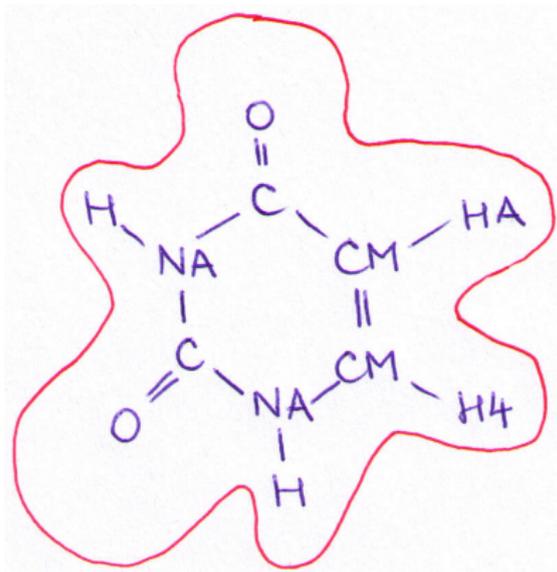
- popular – **potential-derived** charges:
  - 1 calculate the electron density in the molecule
  - 2 get **electrostatic potential** at surface of the molecule
  - 3 **fit** point electric charges on atoms to reproduce the ESP

Possible improvement – **polarizable force field**

- atomic polarizability  $\alpha_i$  is assigned to every atom  $i$
- external field induces atomic dipole  $\vec{\mu}_i = \overleftarrow{\alpha}_i \cdot \vec{E}$

# Coulomb interaction

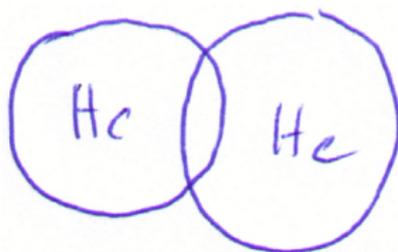
surface of the uracil molecule



# van der Waals interaction

## Pauli repulsion

- electrons with the same spin avoid spatial overlap



- modeling:

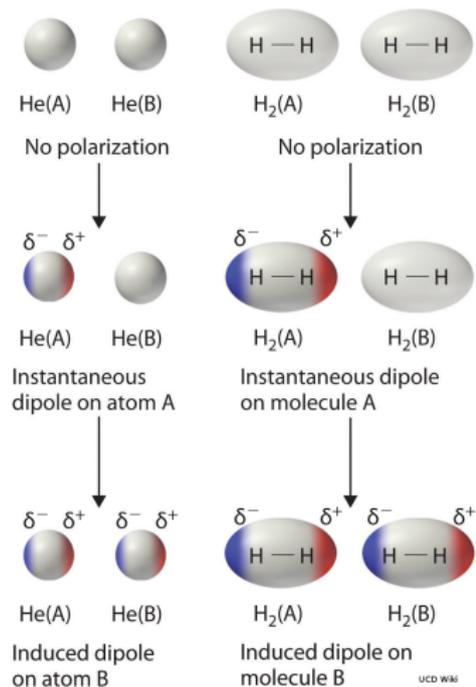
$$E_{\text{ex}} = \exp[a - b \cdot R_{ij}]$$

$$E_{\text{ex}} = \left(\frac{\sigma}{R_{ij}}\right)^{12}$$

# van der Waals interaction

dispersion due to correlation

- correlation – between electrons irrespective of spin, retained on longer distances
- instantaneous dipole  $\rightarrow$  induced dipole  $\rightarrow$  interaction
- orientation of dipoles is correlated – **attractive** interaction
- $R^{-6}$ -dependence, proportional to polarizabilities



# van der Waals interaction

most common function: **Lennard-Jones 12-6** potential

$$V(r) = 4\varepsilon \left( \left( \frac{\sigma}{r} \right)^{12} - \left( \frac{\sigma}{r} \right)^6 \right)$$

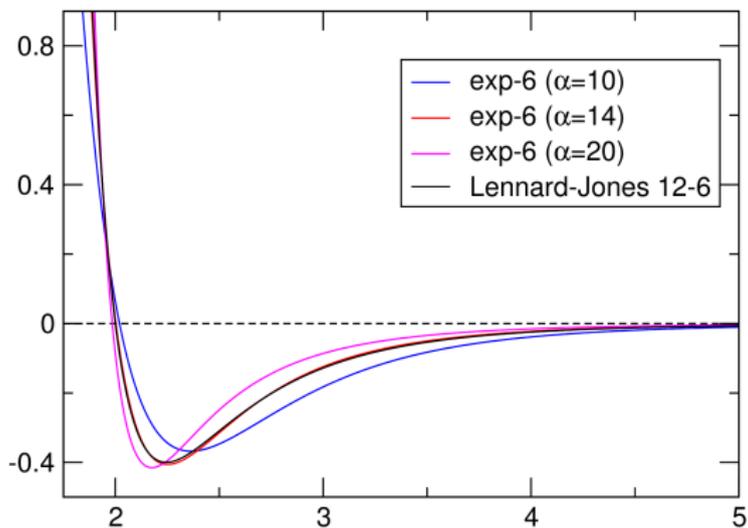
- 2 parameters –  $\sigma$  and  $\varepsilon$

repulsive:  $\exp[-R]$  sometimes better than  $R^{-12} \rightarrow$  **exp-6** potential

- may be a better choice for phase transitions
- e.g. MM water would not freeze below 0 °C with LJ 12-6

note: **phase transitions** are difficult to simulate generally

# van der Waals interaction



# van der Waals interaction

## parametrization

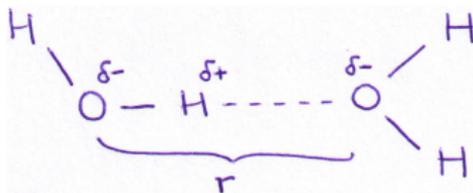
- challenging task in general
- fitting of params to experimental / quantum-chem. data
- e.g. relation to density and heat of vaporization
  - obvious in organic liquids – major interaction

# Hydrogen bonding

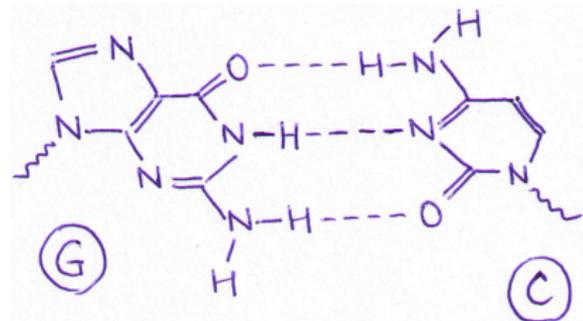
- crucial interaction in biomolecules
- interplay of several kinds of interactions
- typical binding energies: 20 kJ/mol
  - higher for strongly polarized or even charged molecules
  - or if there are several H-bonds (nucleobase pairs)
- early force fields – special potential functions for H-bonding
- modern force fields – no special treatment

# Hydrogen bonding

H<sub>2</sub>O dimer



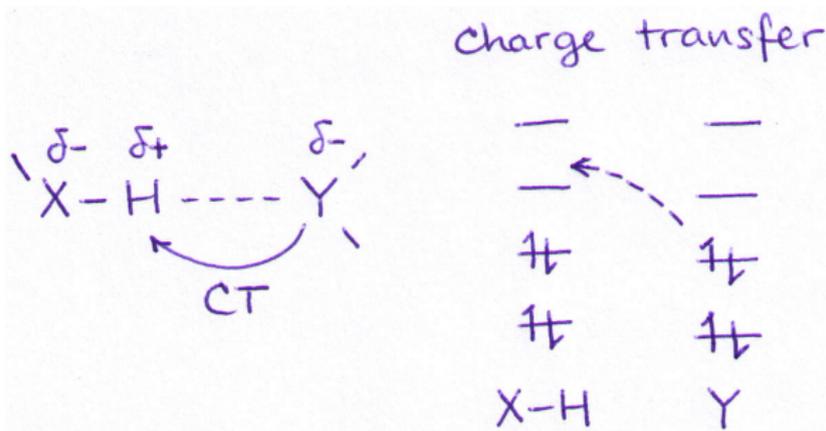
guanine:cytosine base pair



# Hydrogen bonding

- Coulomb interaction is dominant
- vdW interaction
  - may become important, especially in weakly bound systems
  - crucial e.g. for angular dependence in  $\text{H}_2\text{CO} \dots \text{H}_2\text{O}$  etc.
- **charge transfer** contribution
  - cannot be covered by force fields due to constant charges
  - may be included in other terms effectively

# Hydrogen bonding



charge transfer – into the  $\sigma^*$  orbital

→ weakening of the X–H bond → red shift in the IR spectrum

# Parametrization of bonded interactions

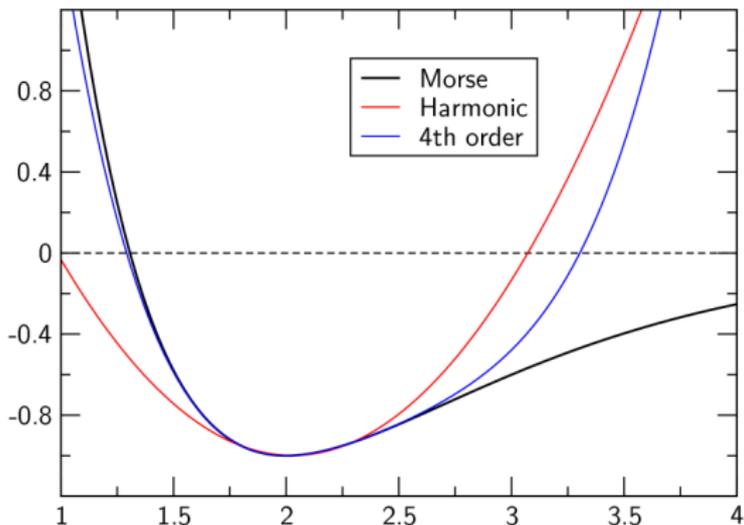
## Bonds

- harmonic approximation (Taylor expansion up to 2nd order)

$$E(r) = \frac{1}{2}k(r - r_0)^2$$

- 2 parameters – equilibrium distance and force constant
- works in a narrow interval of distances
- often sufficient (vibrations are within the interval)
- if bonds are to be created or broken (chemistry)
  - another solution has to be sought
  - probably leave molecular mechanics ☹

# Parametrization of bonded interactions



- for accurate vibration frequencies
  - quartic terms can be important to describe the curvature

# Parametrization of bonded interactions

## Angles

- harmonic approximation for the angle deformation

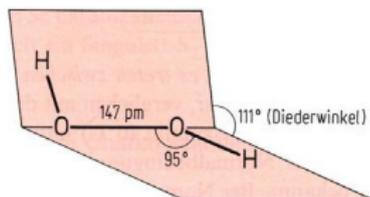
$$E_{\text{bend}}(\vartheta) = \frac{1}{2}k_{\vartheta}(\vartheta - \vartheta_0)^2$$

- 2 parameters needed – equilibrium angle and force constant
- from experiment (vib-rot spectra) or quantum chemistry

# Parametrization of bonded interactions

## Dihedral angles

- describe the rotation around covalent bonds
- defined by 4 atoms



# Parametrization of bonded interactions

## Dihedral angles

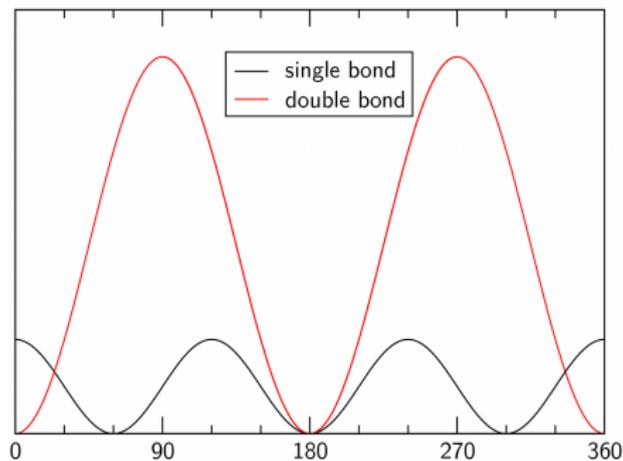
- describe the rotation around covalent bonds
- defined by 4 atoms
- potential energy – periodic function of the dihedral angle:

$$E(\omega) = \sum_{n=1,2,3,4,6} V_n \cos [n \cdot \omega - \gamma_n]$$

- $V_n$  – amplitude (barrier),  $n$  – periodicity,  $\gamma$  – phase shift

# Parametrization of bonded interactions

Dihedral angles – example: C–C single and C=C double bonds



# The complete equation

$$\begin{aligned} E(R^N) &= \\ &= \frac{1}{2} \sum_i k_i (r_i - r_i^0)^2 + \frac{1}{2} \sum_j k_j^\vartheta (\vartheta_j - \vartheta_j^0)^2 + \frac{1}{2} \sum_n V_n \cdot \cos [n\omega - \gamma_n] \\ &+ \sum_i^N \sum_{j=i+1}^N \left\{ 4\varepsilon_{ij} \left( \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ij}} \right)^6 \right) + \frac{1}{4\pi\varepsilon_0} \frac{q_i q_j}{r_{ij}} \right\} \end{aligned}$$

# Molecular dynamics simulation

how to get things moving

# Equations of motion

$$m \cdot \ddot{r} = F$$

ordinary differential equations of 2nd order

- have to be solved numerically
- solution proceeds in discrete **steps** of length  $\Delta t$
- numerical integration starts at time  $t_0$ ,  
where the **initial conditions** are specified
  - the positions  $r_0$  and the velocities  $v_0$
- calculations of forces at  $r_0$  to get accelerations  $a_0$
- then, an integrator calculates  $r$  and  $v$  at time  $t_0 + \Delta t$
- accelerations  $\rightarrow$  step  $\rightarrow$  accelerations  $\rightarrow$  step  $\rightarrow \dots$

# Verlet integration method

a virtual step in positive time and in 'negative' time,  
and Taylor expansion up to 2nd order:

$$r(t + \Delta t) = r(t) + \dot{r}(t) \cdot \Delta t + \frac{1}{2} \ddot{r}(t) \cdot \Delta t^2$$
$$r(t - \Delta t) = r(t) - \dot{r}(t) \cdot \Delta t + \frac{1}{2} \ddot{r}(t) \cdot \Delta t^2$$

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$$r(t - \Delta t) = r(t) - \dot{r}(t) \cdot \Delta t + \frac{1}{2} \ddot{r}(t) \cdot \Delta t^2$$

add both equations – eliminate the velocity  $\dot{r}$ :

$$r(t + \Delta t) = 2 \cdot r(t) - r(t - \Delta t) + \ddot{r}(t) \Delta t^2$$

$$\ddot{r}(t) = a(t) = \frac{F(t)}{m} = -\frac{1}{m} \frac{\partial V}{\partial r}(t)$$

# Verlet integration method

another but equivalent formulation – velocity Verlet

$$\begin{aligned}r(t + \Delta t) &= r(t) + v(t) \cdot \Delta t + \frac{1}{2}a(t) \cdot \Delta t^2 \\v(t + \Delta t) &= v(t) + \frac{1}{2}(a(t) + a(t + \Delta t)) \cdot \Delta t\end{aligned}$$

yet another – Leap-frog

$$\begin{aligned}v(t + \frac{1}{2}\Delta t) &= v(t - \frac{1}{2}\Delta t) + a(t) \cdot \Delta t \\r(t + \Delta t) &= r(t) + v(t + \frac{1}{2}\Delta t) \cdot \Delta t\end{aligned}$$

## $\Delta t$ – crucial parameter

- Let us say: we want to obtain a trajectory over a time interval  $T$
- we perform  $M$  steps
  - we have to evaluate the forces on atoms  $M = T/\Delta t$  times

Computational cost of the calculation of forces

- major computational effort
- determines how many steps we can afford to make

## $\Delta t$ – crucial parameter

- we neglect contributions in  $\Delta t^3$  and higher orders  
→ error per step in the order of  $\Delta t^3$
- keep the step short → make the error small  
but need too many steps to simulate certain time  $T$
- make the step long → cut computational cost  
but increase the error and decrease stability
- compromise needed

## $\Delta t$ – crucial parameter

- fastest motion – hydrogen atoms, period around 10 fs
- rule of thumb – stable integration with  $\Delta t \leq \frac{1}{10}$  fastest period
- practically,  $\Delta t$  of 1 fs is used (2 fs with special treatment)
- 1M calculations of forces needed for a trajectory of 1 ns
- large systems – multi-ns simulations routinely,  $\mu s$  possible

# Introducing thermodynamics

what you simulate is what you would measure

# Intro

Solution of equations of motion – conserves total / internal energy

what we need – to control basic simulation parameters

– temperature and possibly pressure

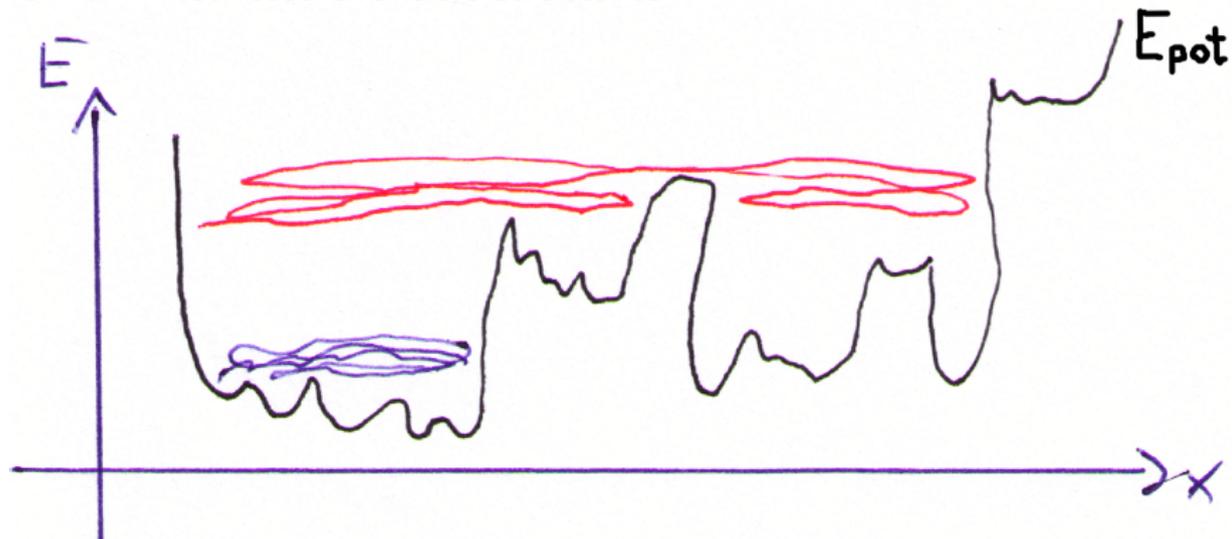
significance of temperature

– determines which structures of the system are accessible

– different dynamics at high and at low temperatures

# Intro

high  $E$  – multiple different structural ‘classes’ are reached  
low  $E$  – restricted available structures



difference  $E - E_{pot}$  corresponds to  $E_{kin}$  and temperature

# Isolated system

- exchanges with surroundings neither energy (heat / work) nor matter (particles)
- total energy of system:  $E = E_{\text{kin}} + E_{\text{pot}} = \text{const}$
- individually,  $E_{\text{kin}}$  and  $E_{\text{pot}}$  fluctuate in the course of time as they are being transformed into each other
- is what we get when using the Verlet method for a molecule

kinetic theory of gases  $\rightarrow$  relation of  $E_{\text{kin}}$  and temperature:

$$\langle E_{\text{kin}} \rangle = \frac{3}{2} NkT$$

where  $\langle E_{\text{kin}} \rangle = \frac{1}{2} \sum_i m_i \langle v_i^2 \rangle$

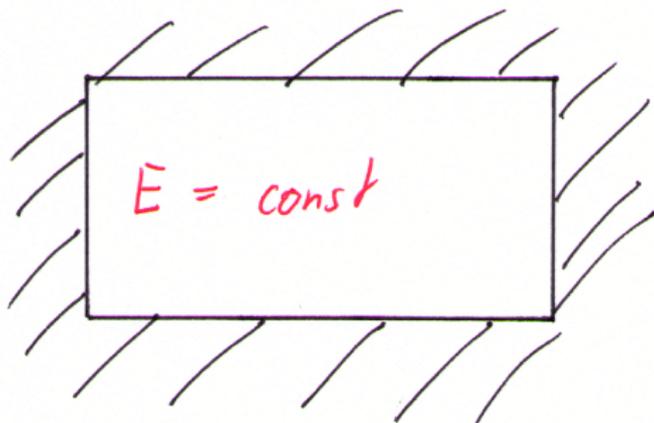
'local'  $T$  – fluctuates in time; may differ between parts of system

# Isolated and closed system

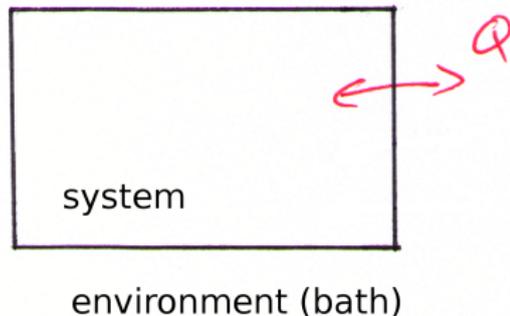
experimental setup (a test tube with a sample)

- usually in **thermodynamic equilibrium** with the surroundings
- temperature (and opt. pressure) equal as that of surr.

isolated system



closed system

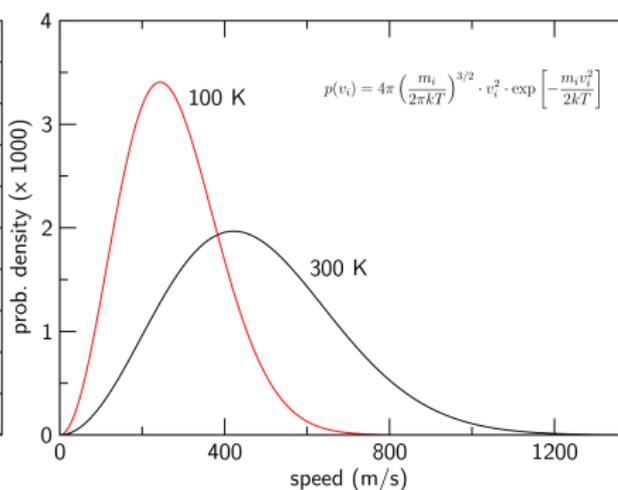
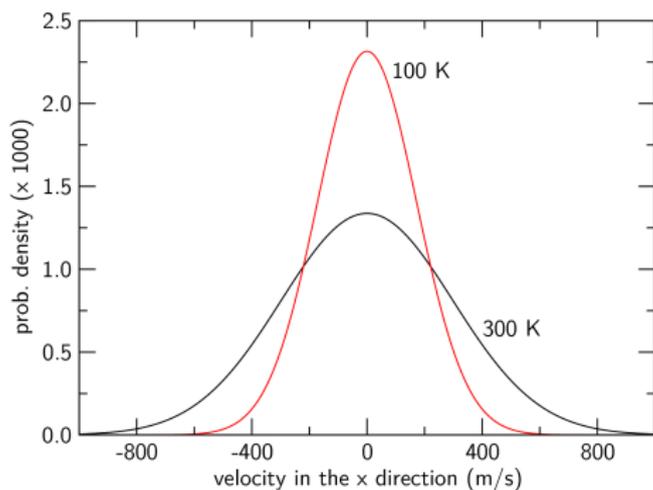


## Closed system

- thermal contact of system with surroundings
- exchange of energy in the form of heat  
until the temperature of surroundings is reached
- **canonical ensemble**
- velocity / speed of atoms – Maxwell–Boltzmann distribution

# Canonical ensemble

## Maxwell–Boltzmann distribution of velocity / speed ( $N_2$ , IG)



# Naïve thermostat – scaling of velocities

in a Verlet MD simulation – ‘instantaneous temperature’  $T$   
deviates from the target  $T_{\text{ref}}$  (of bath = the surroundings)

$$T(t) = \frac{2}{3} \frac{E_{\text{kin}}(t)}{Nk} \neq T_{\text{ref}}$$

$T(t)$  – another name for  $E_{\text{kin}}$  determined by velocities  
simple idea – **scale** the velocities by a certain factor  $\lambda$ :

$$\begin{aligned} T_{\text{ref}} &= \frac{1}{\frac{3}{2}Nk} \cdot \frac{1}{2} \sum_i m_i (\lambda \cdot v_i)^2 = \\ &= \lambda^2 \cdot \frac{1}{\frac{3}{2}Nk} \cdot \frac{1}{2} \sum_i m_i v_i^2 = \lambda^2 \cdot T \end{aligned}$$

## Naïve thermostat – scaling of velocities

scaling of all velocities by  $\lambda = \sqrt{T_{\text{ref}}/T} \rightarrow T_{\text{ref}}$  reached exactly

- rescaling the velocities affects the ‘natural’ way of evolution of the system
- velocities – not sure if the distribution is correct (M–B)
- importantly, system does not sample any canonical ensemble – very important because everything is calculated as averages:

$$\langle A \rangle = \frac{1}{Z} \int \rho \cdot A \, d\vec{r} \, d\vec{p}$$

- possibly: wrong sampling  $\rightarrow$  wrong averages

## Berendsen thermostat

How to avoid the drastic changes to the dynamics?

adjust velocities more smoothly, in the direction of  $T_{\text{ref}}$

- temperature changes between two time steps according to

$$\Delta T = \frac{\Delta t}{\tau} (T_{\text{ref}} - T)$$

- rate of change of  $T$  (due to the change of velocities)  
is proportional to the deviation of actual  $T$  from  $T_{\text{ref}}$
- constant of proportionality – relaxation time  $\tau$

# Berendsen thermostat

- velocities are scaled by  $\lambda$ :

$$T_{\text{new}} = T + \Delta T = T + \frac{\Delta t}{\tau} (T_{\text{ref}} - T)$$
$$\lambda = \sqrt{\frac{T_{\text{new}}}{T}} = \sqrt{1 + \frac{\Delta t}{\tau} \left( \frac{T_{\text{ref}}}{T} - 1 \right)}$$

- usually:  $\tau = 0.1 - 10$  ps
- $T$  will fluctuate around the desired value  $T_{\text{ref}}$
- **problem** – still does not generate correct canonical ensemble

## Nosé–Hoover thermostat

- represents rigorously the canonical ensemble  $\rightarrow$  ideal choice
- conceptionally and mathematically  $>$  difficult to understand
- heat bath is treated not as an external element  
rather as an integral part of the system  
is assigned an additional DOF  $s$  with fictitious mass  $Q$
- eqns of motion for this **extended system** ( $3N + 1$  DOF):

$$\ddot{r}_i = \frac{F_i}{m_i} - s \cdot \dot{r}_i$$
$$\dot{s} = \frac{1}{Q} (T - T_{\text{ref}})$$

# Temperature and thermostats

**fluctuation** of temperature – desired property  
for canonical ensemble – **variance** of ‘inst. temperature’  $T$ :

$$\sigma_T^2 = \langle (T - \langle T \rangle)^2 \rangle = \langle T^2 \rangle - \langle T \rangle^2$$

and relative variance

$$\frac{\sigma_T^2}{\langle T \rangle^2} = \frac{2}{3N}$$

large number of atoms  $N$ : fluctuations  $\rightarrow 0$   
finite-sized systems: visible fluctuation of temperature  
– is correct (feature of the canonical ensemble)

# Introducing pressure

chemical reality – constant pressure rather than constant volume  
goal – implement such conditions in simulations, too

How to calculate pressure? – first, calculate **virial of force**

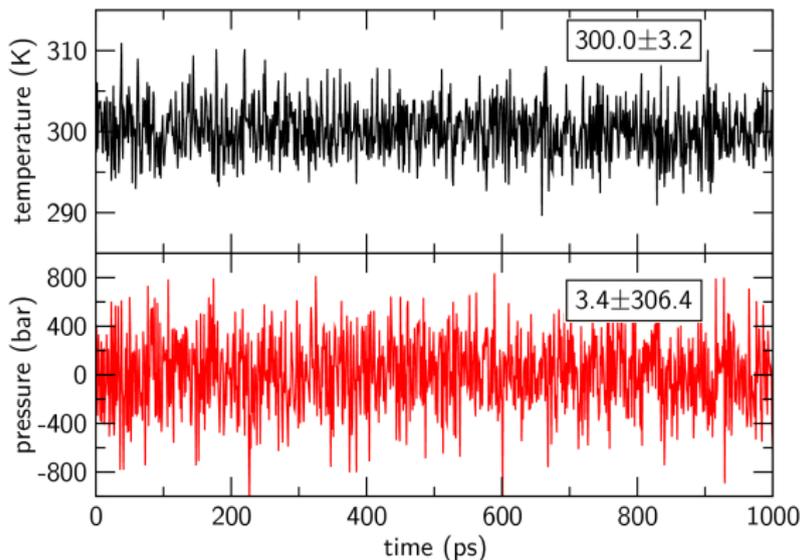
$$\Xi = -\frac{1}{2} \sum_{i < j} \vec{r}_{ij} \cdot \vec{F}_{ij}$$

( $\vec{r}_{ij}$  distance of atoms  $i$  and  $j$ ,  $\vec{F}_{ij}$  – force between them)

$$P = \frac{2}{3V} \cdot (E_{\text{kin}} - \Xi) = \frac{2}{3V} \cdot \left( \frac{1}{2} \sum_i m_i \cdot |\vec{v}_i|^2 + \frac{1}{2} \sum_{i < j} \vec{r}_{ij} \cdot \vec{F}_{ij} \right)$$

# Measuring pressure

$T$  and  $P$  in an NPT simulation of a DNA oligomer in water  
( $T_{\text{ref}} = 300$  K,  $P_{\text{ref}} = 1.0$  bar)



# Controlling pressure

we can **calculate** the pressure

– so how do we **maintain** it at a constant value?

**barostat** – algorithm that is equivalent of a thermostat,  
just that it varies **volume** of the box instead of velocities

alternatives are available:

- Berendsen barostat
  - direct rescaling of box volume
  - system coupled to a ‘force / pressure bath’ – piston
- Parrinello–Rahman barostat
  - extended-ensemble simulation
  - additional DOF for the piston